

of front tire, z_3 is the vertical displacement of back tire; $y = \xi + w$, ξ is the bridge deck roughness value, w is the bridge corresponding dynamic deflection in the place of tire.
The vehicle system vibration differential equation is given by:

$$\begin{cases} m_1 \ddot{z}_1 + (c_{s1} + c_{t1}) \dot{z}_1 - c_{s1} \dot{z}'_1 + (k_{s1} + k_{t1}) z_1 - k_{s1} z'_1 = m_1 g + k_{t1} y_1 + c_{t1} \dot{y}_1 \\ m_2 \ddot{z}_2 + (c_{s2} + c_{t2}) \dot{z}_2 - c_{s2} \dot{z}'_2 + (k_{s2} + k_{t2}) z_2 - k_{s2} z'_2 = m_2 g + k_{t2} y_2 + c_{t2} \dot{y}_2 \\ (Mb_2^2 + I_a / l_v^2) \ddot{z}'_1 + (Mb_1 b_2 - I_a / l_v^2) \ddot{z}'_2 - c_{s1} \dot{z}_1 + c_{s1} \dot{z}'_1 - k_{s1} z_1 + k_{s1} z'_1 = M g b_2 \\ (Mb_1 b_2 - I_a / l_v^2) \ddot{z}'_1 + (Mb_1^2 + I_a / l_v^2) \ddot{z}'_2 - c_{s2} \dot{z}_2 + c_{s2} \dot{z}'_2 - k_{s2} z_2 + k_{s2} z'_2 = M g b_1 \end{cases} \quad (1)$$

Where $y_1 = y(x_1)$, $y_2 = y(x_2)$ is the deck roughness value in the place of front and back axle, respectively, \dot{z}_i , \dot{z}'_i , \dot{y}_i ($i=1,2$) is the corresponding speed, \ddot{z}_i , \ddot{z}'_i , \ddot{y}_i ($i=1,2$) is the corresponding acceleration, $\ddot{\alpha}$ is the angular acceleration, ϵ is the variation of virtual displacement.

Put the deck roughness sequence in the form of $\xi(x)$ into Eq. (1), and solve Eq. (1) using Wilson - θ method. Then, the vibration response of vehicle under the condition of different bridge deck grades and different vehicle speeds can be obtained.

The interaction force between vehicle and bridge can be expressed as follows:

$$p_i(t) = k_{i1}(z_{i1} - y_i) + c_{i1}(\dot{z}_{i1} - \dot{y}_i) \quad (i=1, 2) \quad (2)$$

The bridge dynamic response can be solved by finite element method.

3. Dynamic response analysis of simply-supported beam and continuous beam

The parameters of simply-supported beam are listed as follows: its span $L=32m$, its unit length mass $m=5.41 \times 10^3 kg \cdot m^{-1}$, its flexural rigidity $EI = 3.5 \times 10^{10} N \cdot m^2$. According to JTG D60-2004(General Code for Design of Highway Bridge and Culverts), the impacting factor of the beam is 1.2245.

The parameters of vehicle are listed as follows: $M = 38500 kg$; $I_a = 2.446 \times 10^6 kg \cdot m^2$; $l_v = 8.4m$; $b_1 = b_2 = 0.5$; $m_1 = m_2 = 4330 kg$; $k_{s1} = k_{s2} = 2.535 \times 10^6 N \cdot m^{-1}$; $k_{t1} = k_{t2} = 4.28 \times 10^6 N \cdot m^{-1}$; $c_{s1} = c_{s2} = 1.96 \times 10^3 kg \cdot s^{-1}$; $c_{t1} = c_{t2} = 9.8 \times 10^4 kg \cdot s^{-1}$.

The study shows that the impacting factor increases when the bridge deck become rougher. The impacting factor increases from 1.05 (the smooth bridge) to 2.28 (grade D bridge), it has increased 117.1%.

The parameters of continuous beam are listed as follows: $L=3 \times 25m$, $EI=3.2 \times 10^{10} N \cdot m^2$, $m = 9.375 \times 10^3 kg \cdot m^{-1}$. According to the code, the impacting factor is 1.2209.

The study shows that when the vehicle passes near the mid-span of first span, the maximum impacting factor of mid-span of second span happens. But the maximum impacting factor of mid-span of first span happens when the vehicle passes near the mid-span of second span. The impacting factor in mid-span of second span increases from 1.06 (smooth bridge) to 2.03 (grade D bridge), it increases 91.5%. The impacting factor in mid-span of first span increases from 1.08(smooth bridge) to 2.16 (grade D bridge), and it increases 100%. So, the condition of bridge deck is a very important factor affecting the vibration response of bridge.

4. Conclusion

According to the PSD function, the corresponding bridge roughness sequence is established. Using 1/2-four degree vehicle vibration model, the bridge response can be obtained with different bridge roughness. The conclusion can be drawn as follows:

- (1) The deck roughness of bridge is a very important factor for vehicle-bridge interaction. As the bridge deck becomes worse, the vibration of bridge caused by vehicle increase rapidly. And it is more obvious for the simply-supported beam than that of continuous beam.
- (2) The remarkable factor which affects bridge impacting factor is bridge deck grade. In the same vehicle speed, the value of impacting factor increases non-linearly when the grade of bridge deck roughness becomes worse.
- (3) Generally speaking, the highway road spectrum is grade A,B and C in China, and the majority belong to the grade B and C. The impacting factor of grade B for simply-supported beam and grade C for continuous beam is greater than those obtained by the code. So, it is very important to pay more attention to the highway maintenance.